

## In this Chapter Design methodologies for large combinational circuits Bit-parallel Bit-serial

- Integer arithmetic as examples
- Add, subtract, multiply, and divide as four basic arithmetic operations
- IEEE floating-point number standards
- Floating-point Data Space
- Floating-point arithmetic
- Floating-point unit (FPU)



#### Carry Look-Ahead (CLA) **Adder** FA expression from Ch2: • Goal: Generate carry bits in parallel $s_i = a_i \oplus b_i \oplus c_{i-1}$ • Let's examine FA expressions $c_i = (a_i \oplus b_i) c_{i-1} + a_i b_i$ • Easy to generate p and g bits in parallel Let. • Carry bits are dependent, but can $p_i = a_i \oplus \ b_i$ substitute carry expressions to break $g_i = a_i b_i$ dependency • Once carry bits are known, easy to $s_i = p_i \oplus c_{i-1}$ generate sum bits in parallel $c_i = g_i + p_i c_{i-1}$ • ΔCLA(8) = ? 0.8 ns













### Example ALU Modules

- Design Arithmetic module
  - Use n-bit 2's complement adder/subtractor
  - Left input always A
  - Right input either B or 1
  - Need a circuit that outputs B if add/sub or 1 if inc/dec.
    Use known modules when possible
- Design n-bit 4-to-1 MUX
  - Bit-parallel: Design using n-bit 2-to-1 MUXs (bit-parallel)
  - Bit-serial: Design using 1-bit 4-to-1 MUX slices
- Design Map and Mask circuits
   Create truth tables
  - Find minimal SOP/POS expressions







# Real Number Arithmetic EEE 754 FP number Standards Single, 32 bits 1-bit sign, 8-bit biased exponent (bias = 127), 23-bit fraction Stored as a 32-bit number in memory double, 64 bits 1-bit sign, 11-bit biased exponent (bias = 1023), 52-bit fraction Stored as a 64-bit number in memory Extended, 80 bits 1-bit sign, 15-bit bias exponent (bias = 16383), 64-bit fraction Stored in 80-bit registers only (no memory representation)



#### Data Space Illustration (1-Dimensional)

- Bold and thin lines indicate real numbers stored as FP numbers in computer
- More fraction bits implies more thin lines
- More exponent bits implies more bold lines







Based on the value of the bits lost
May require another normalization step



